

The chemistry between Newton and Schrodinger

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“Those who educate children well are more to be honored than they who produce them; for these only gave them life, those the art of living well.”

- Aristotle (384-322 BCE)

“To me there has never been a higher source of earthly honor or distinction than that connected with advances in science.”

– Sir Isaac Newton (1642-1727)

Outline

- Why are we talking about this?
 - Understanding the world around us
 - Nobel Prize!
- The classical world through two slits
 - Particles: Newton, Lagrange and Hamilton
 - Waves: Huygens, Young
- It's 1926 and the world gets stranger: quantum mechanics
 - Bohr, Einstein, Schrodinger, Heisenberg, Born, Dirac, and Feynman
- Chemistry: a foot in two worlds

The Nobel Prize in Chemistry 2013

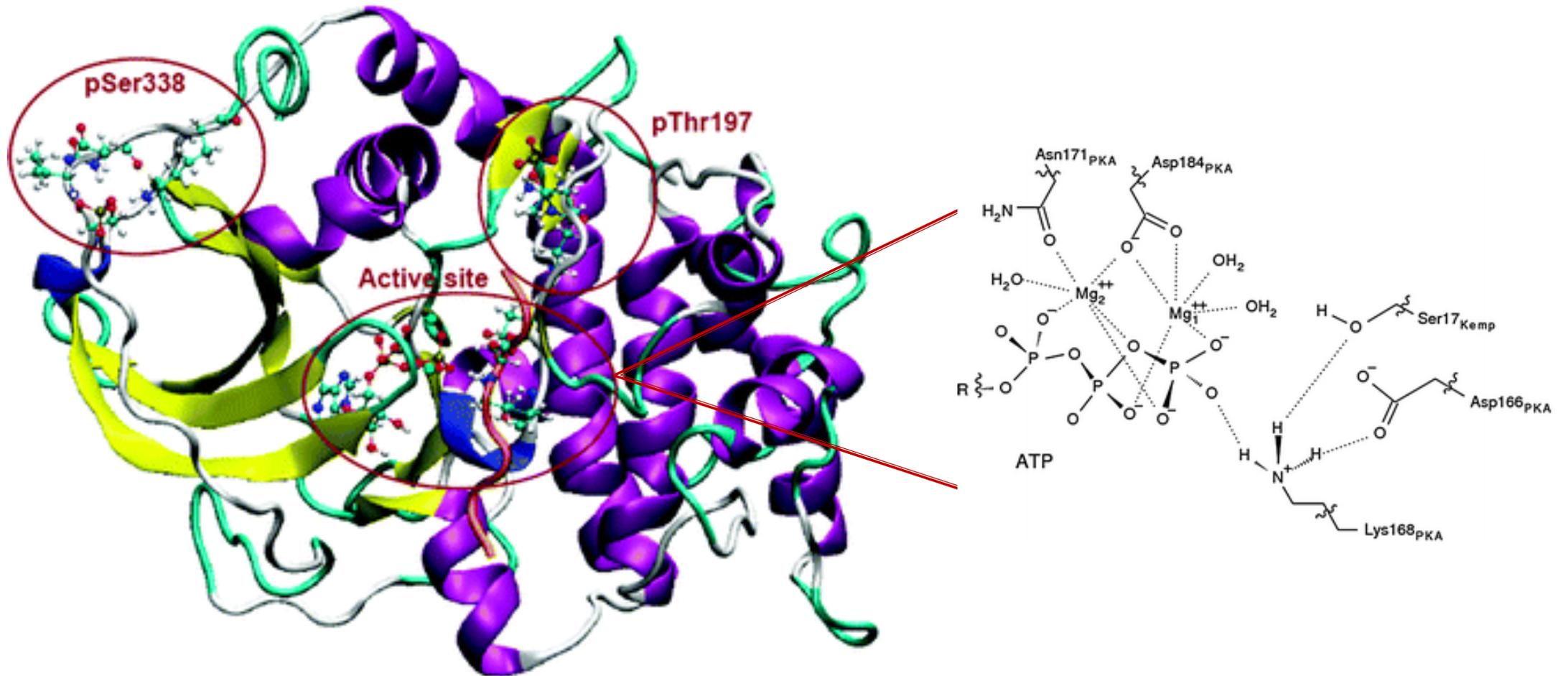
“for the development of multiscale models for complex chemical systems”



Arieh Warshel (USC), Michael Levitt (Stanford Medicine), Martin Karplus (Harvard)

“...they managed to make Newton’s classical physics work side-by-side with the fundamentally different quantum physics.”

QM/MM study of protein kinase



Protein Kinase facilitates transfer of a phosphate (PO_4^-) group:
relevant to many auto-immune disorders

Newton and Schrödinger's cat



The methods of scientific research

- Unify: seek the underlying physics that unites disparate theories



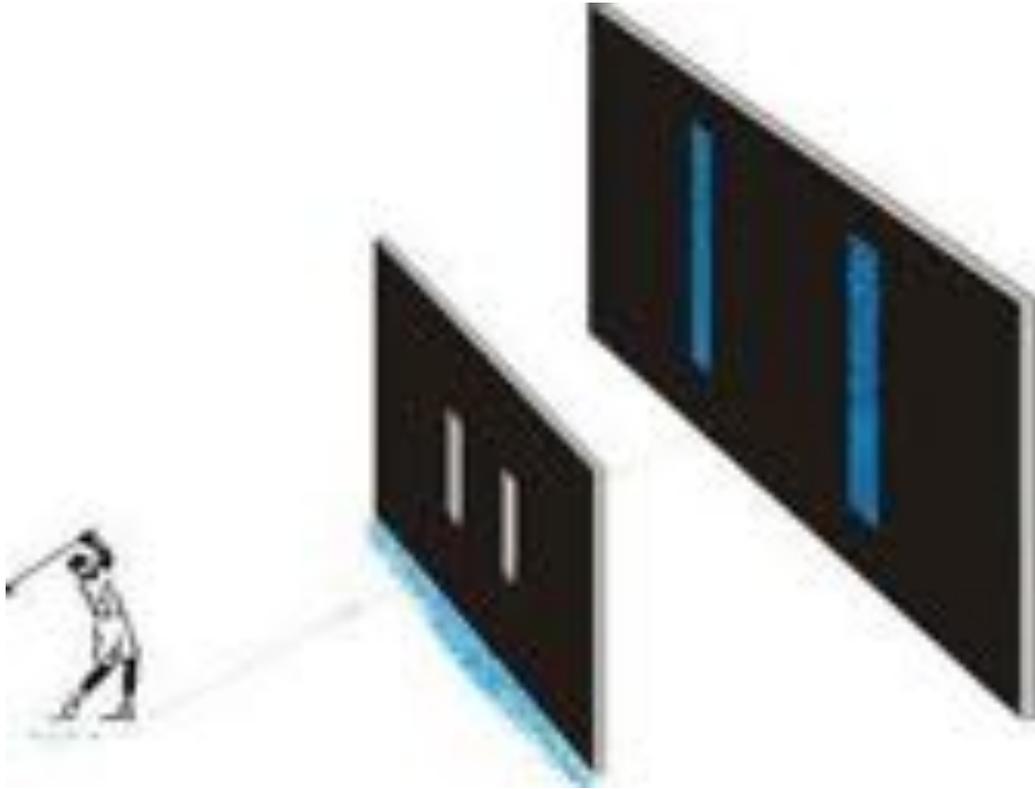
- Reformulate: understand an existing theory in a different way



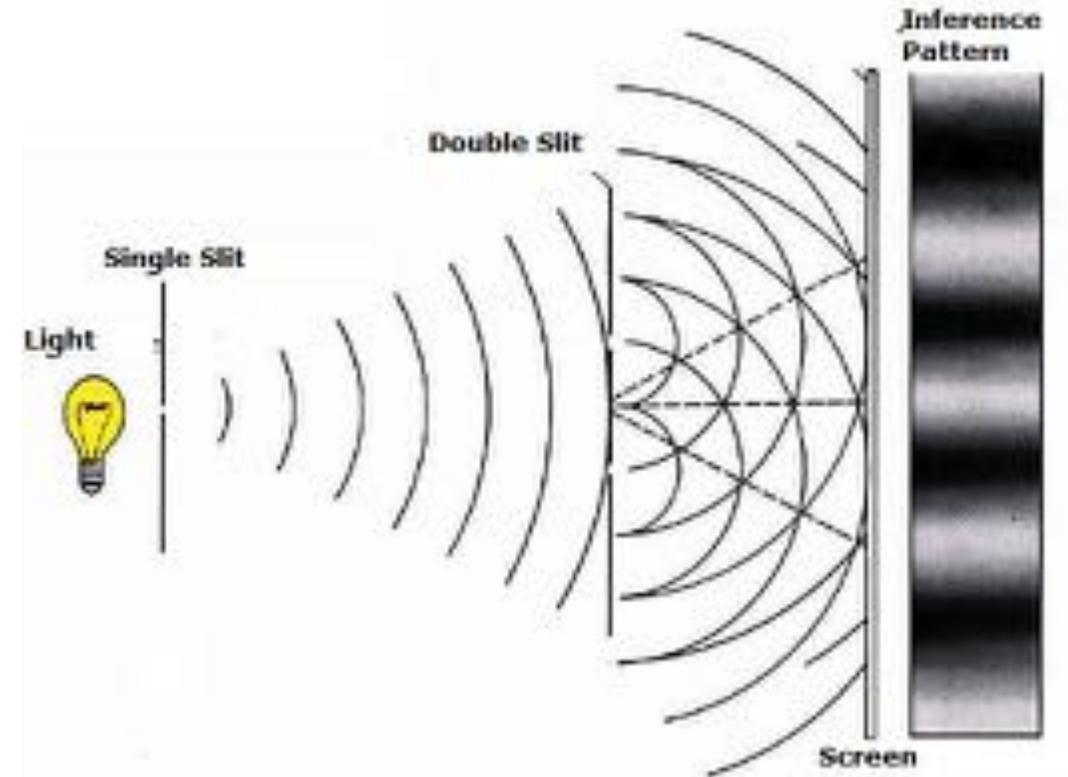
- Discover limits: identify new phenomena transcending current theories



Classical double slit experiment



Classical Particles



Classical Waves

Thomas Young, 1803: set out to disprove Newton's corpuscular theory in favor of Huygen's wave theory of light.

Things start to be 'quantum'

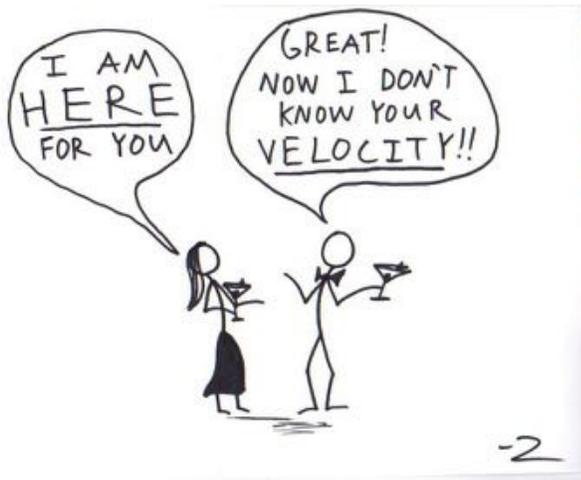
- Boltzmann (1877): energy levels of molecules may be discrete
- Heinrich Hertz and Einstein (1887): photoelectric effect
- Max Planck (1900): black-body radiation
- Neils Bohr (1913): on the constitution of atoms and molecules
- Louis Debroglie (1924): wave-particle duality
- 1926: Heisenberg develops matrix mechanics
Schrödinger publishes wave equation



Life after 1926

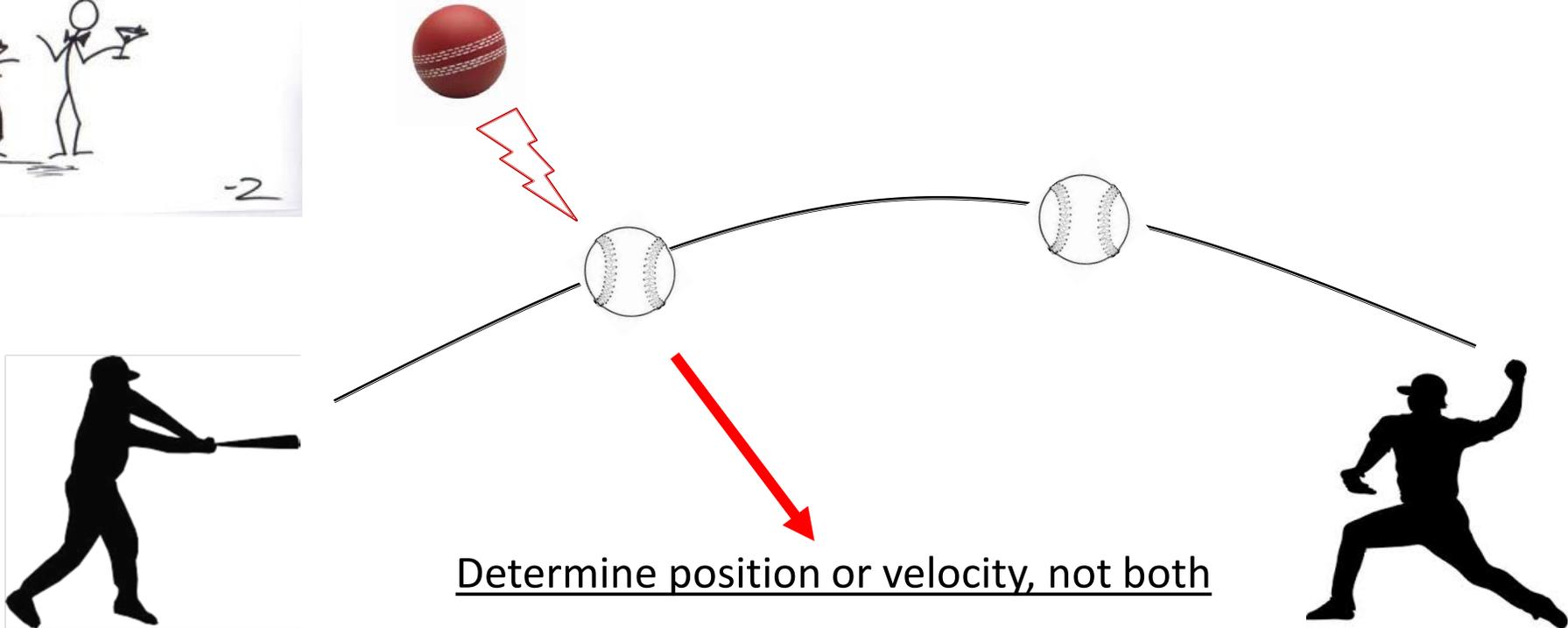
- 1927: Heisenberg uncertainty principle
Dirac brings together QM and Einstein's special relativity
Heitler and London pioneer quantum chemistry
- 1927-1940: Dirac, Pauli, Feynman – Quantum Field Theory
- 1975: Politzer, Gross and Wilczek – Quantum Chromodynamics
- 1979: Weinberg, Salam and Glashow – unified electroweak forces
- 2013: Confirmation of Standard model – theory of almost everything



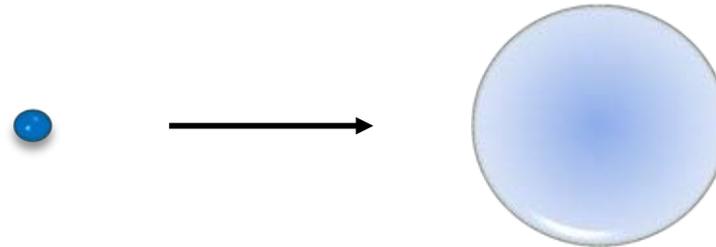


Uncertainty principle

Consequence of Wave-Particle Duality!

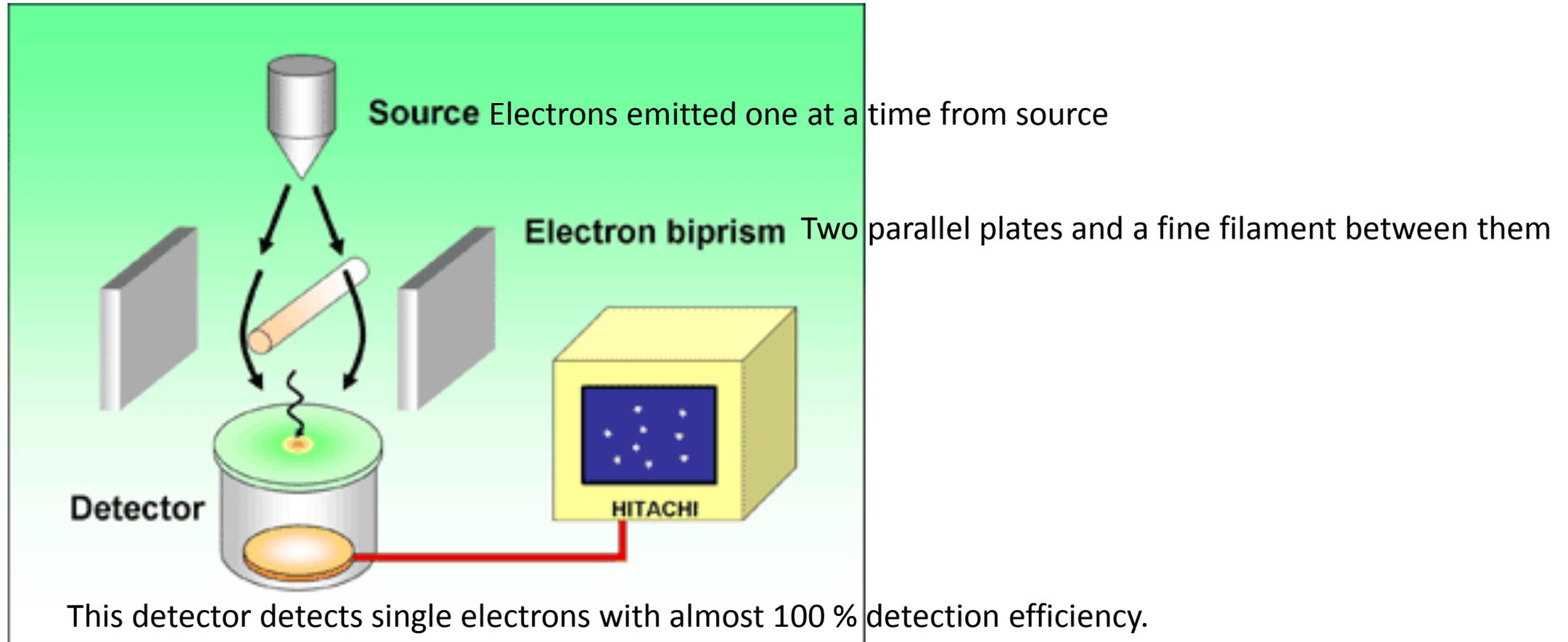


Determine position or velocity, not both



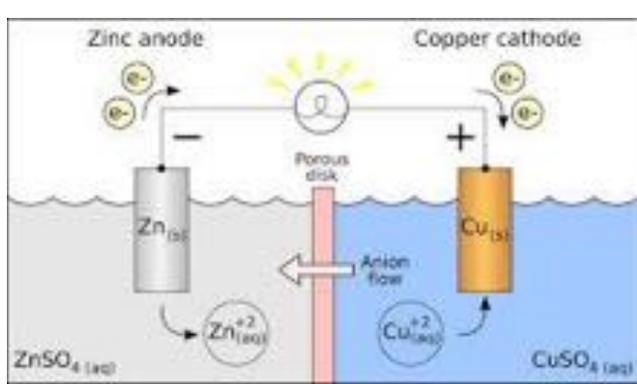
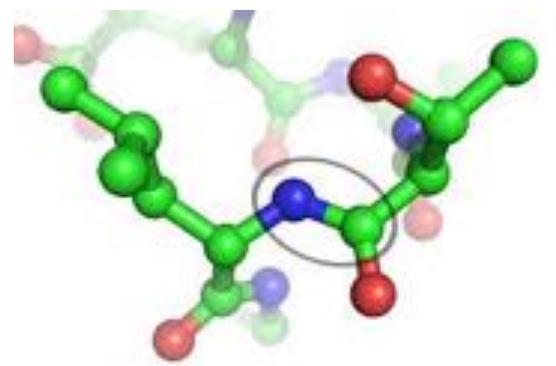
I, at any rate, am convinced that *He* does not throw dice - Einstein

Performing the quantum double-slit experiment



Electron double-slit experiment

Connection to Chemistry?



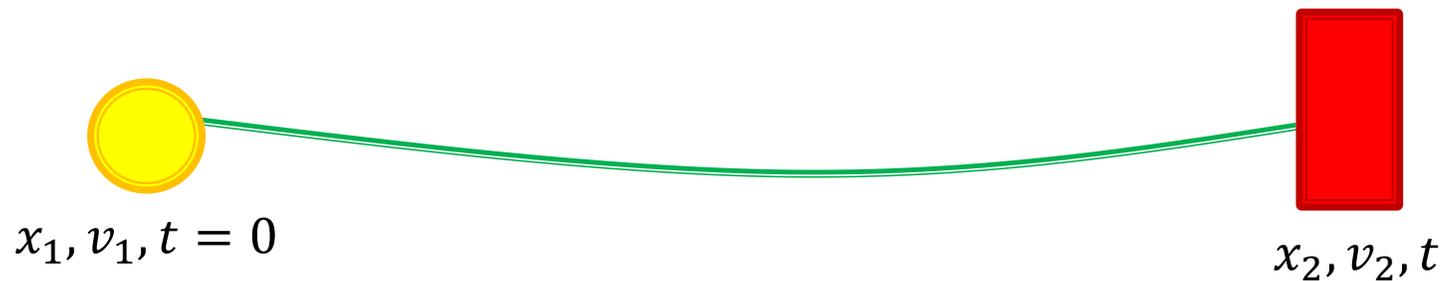
- Chemical reactions involve breaking, making, and changing bonds
- Changing bonds involves moving electrons and atoms: quantum mechanics.
- For bonds not explicitly involved in chemical reaction: classical mechanics.

What is a clever way to combine the two in one uniform framework?

Classical mechanics

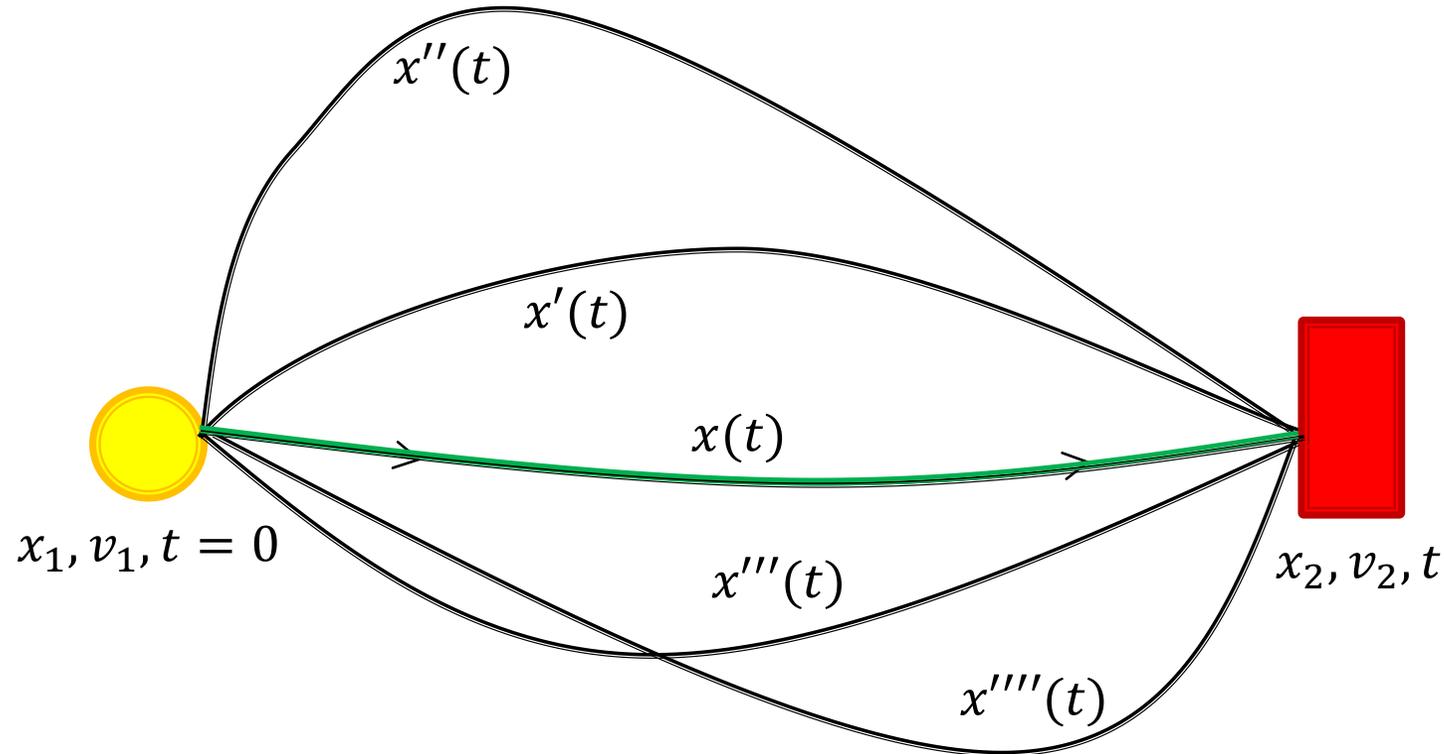
- Deterministic paths
 - Initial position
 - Initial velocity
 - Forces

- Newton's second law: $F = ma$

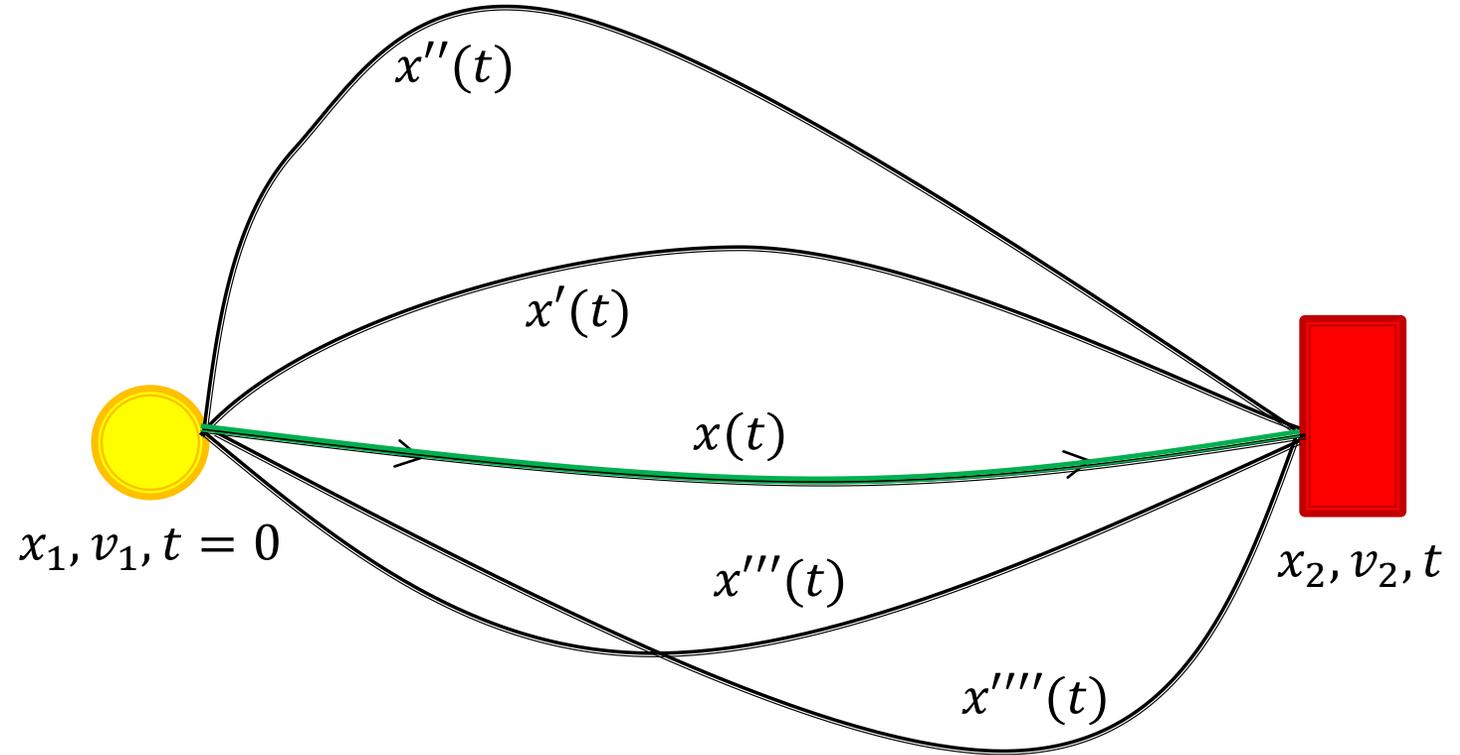


Reformulate: Lagrange and Hamiltonian

- Lagrange introduce action: associate $S[x(t)]$ with classical path $x(t)$
- Hamilton's principal of least action: $\delta S = 0$



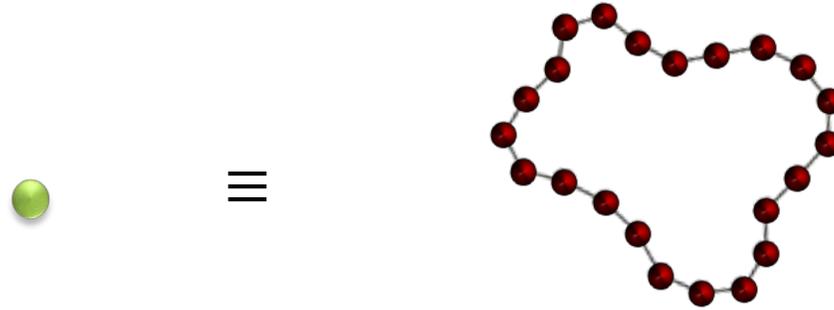
Unify ideas: Feynman Path Integral



$$P((x_1, v_1, t = 0) \rightarrow (x_2, v_2, t)) \propto \sum_{\text{paths}} e^{\frac{iS[x_{\text{path}}(t)]}{\hbar}}$$

Path-Integral representation of quantum mechanics

- A quantum particle behaves like a collection of classical particles



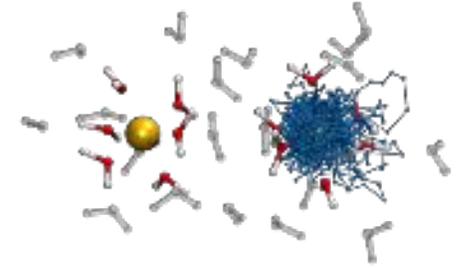
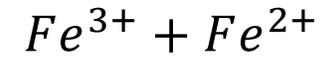
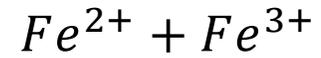
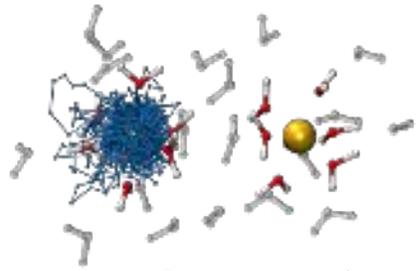
- A quantum particle that behaves like 1 classical particle is a classical particle
- The number of classical particles that describe a quantum particle depends on temperature and/or energy

Dynamics of electron in water

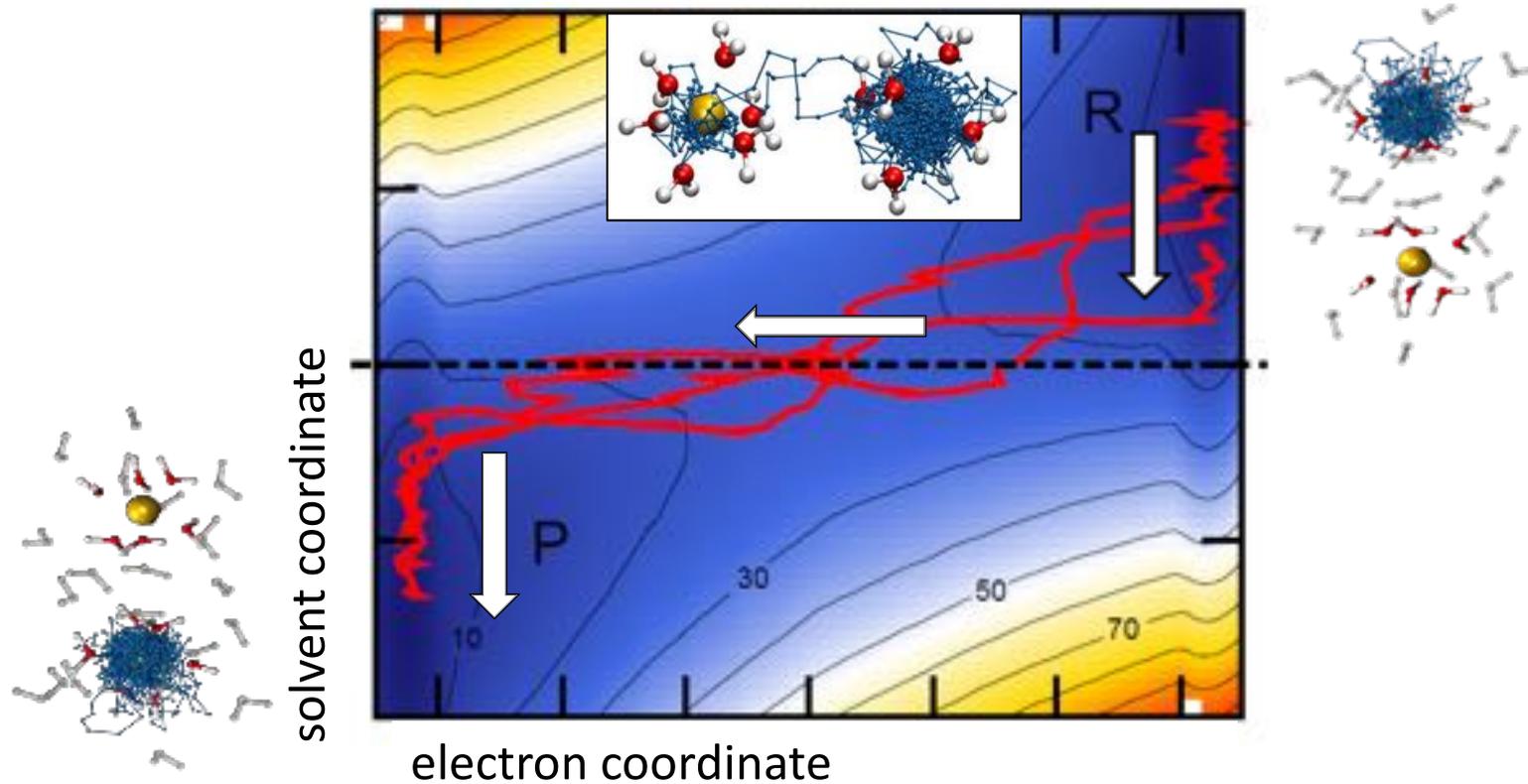
Solvated electron problem: important for all charged particle moving through solvent.

Applications: Battery and electrode design, charge transfer in condensed-phase reactions and many more.

Electron transfer in solution



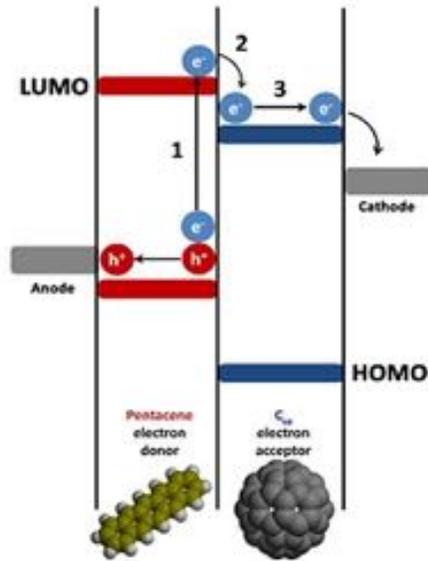
System size: 430 water molecules, 2 metal ions, 1024 path-integral 'beads' for electron.



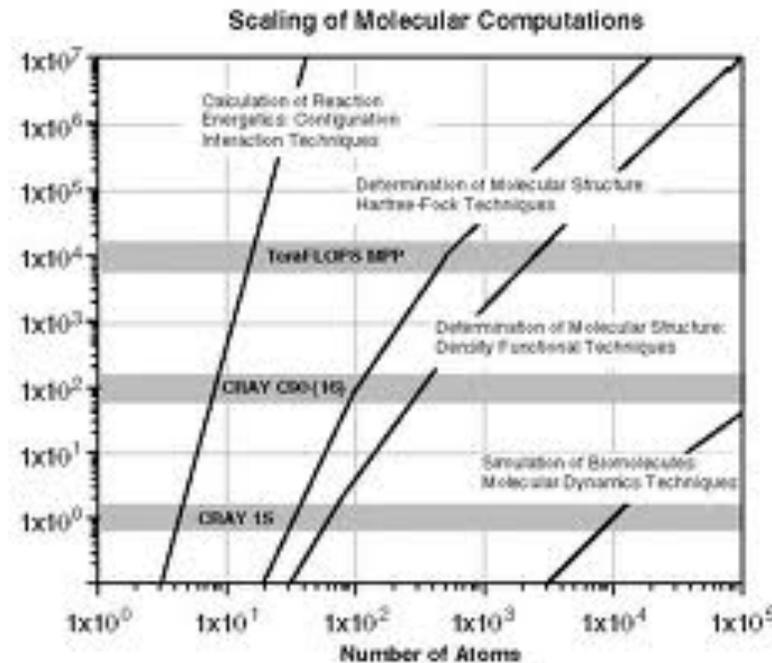
Current research in theoretical chemistry



- Understanding structure-function relations in Biological systems



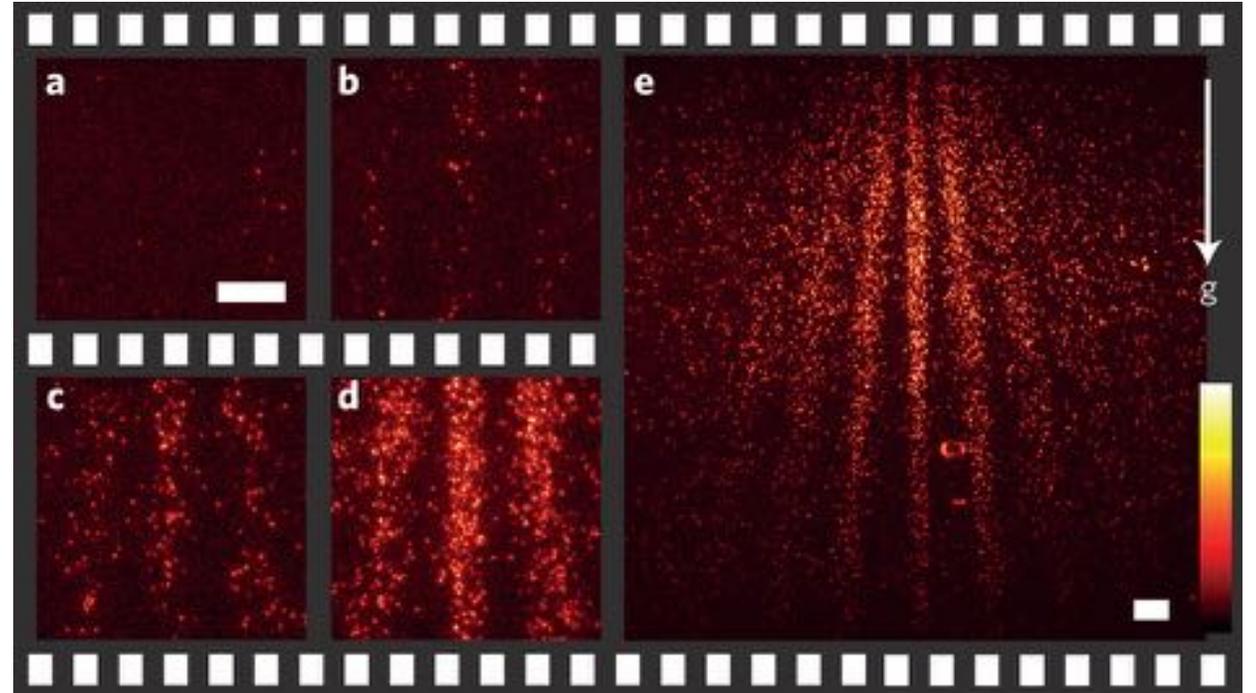
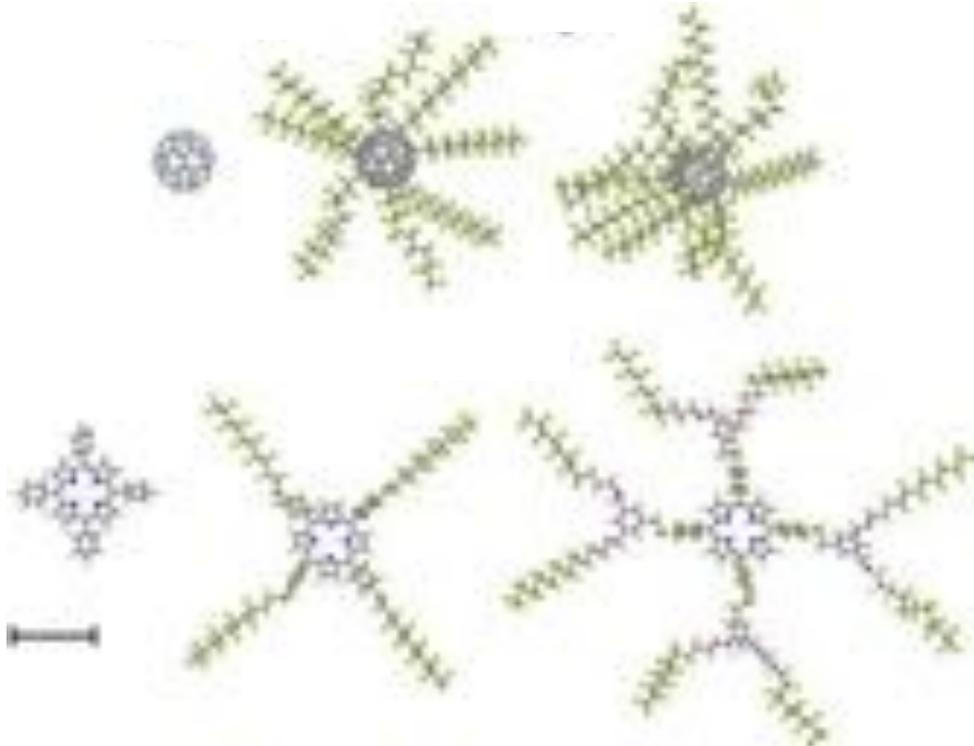
- Designing efficient renewable energy materials



- Computational complexity challenges

Frontiers in quantum mechanics

How big is 'classical'?

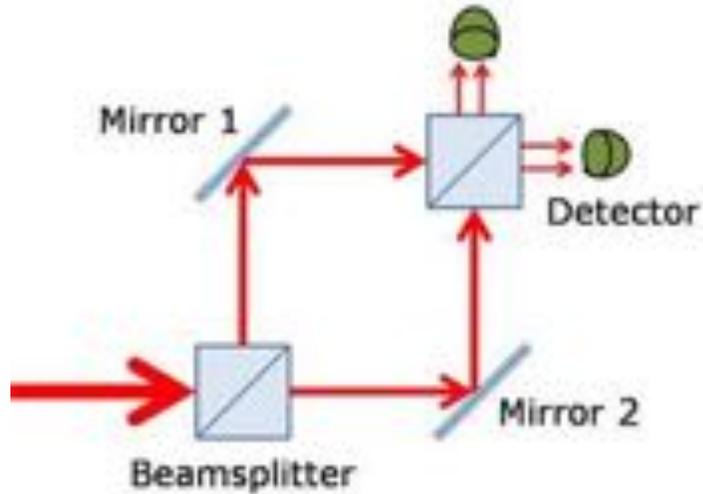


S. Gerlich et al, "Quantum interference of large organic molecules", *Nature* 2, 263 (2011).

T. Juffmann et al, "Real-time single molecule imaging of quantum interference", *Nature Nanotechnology*, 7, 297 (2012).

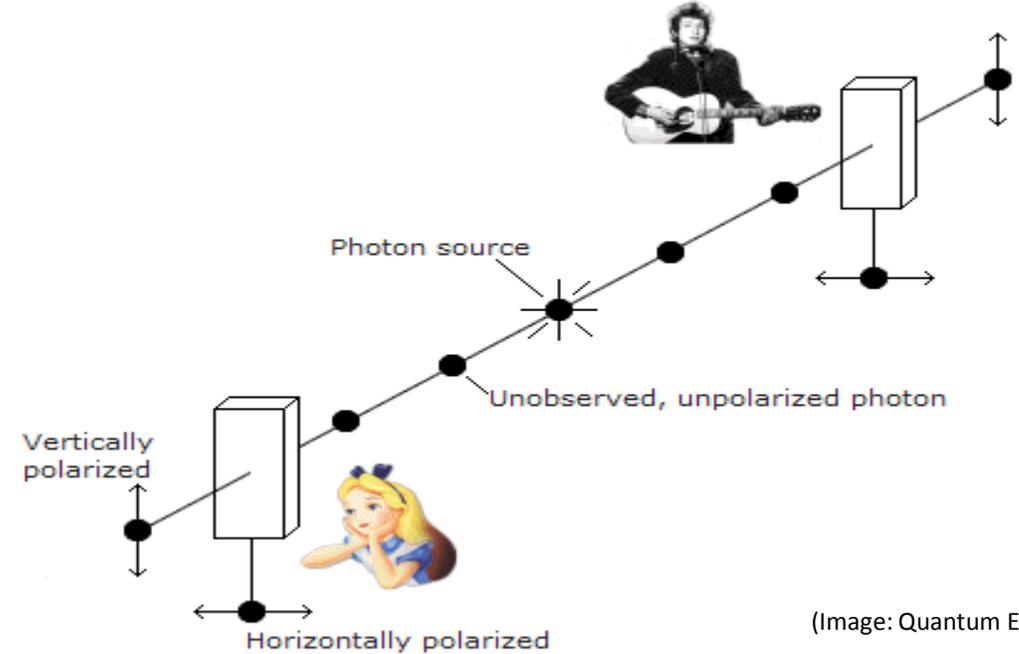
Frontiers in quantum mechanics

Role of observer: double-slit experiment



V. Jacques et al, "Experimental Realization of Wheeler's Delayed-Choice Gedanken Experiment", Science 315, 966 (2007).

Einstein-Podolsky-Rosen (EPR)



(Image: Quantum Enigma)

Quantum mechanical origin of gravity

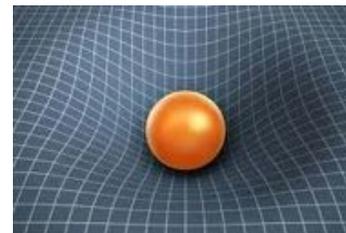


Image: koya/shutterstock

‘Therefore, just as the doctor is said to heal a patient through the activity of nature, so a man is said to cause knowledge in another through the activity of the learner’s own natural reason and this is teaching’

- Thomas Aquinas (1225-1274)

THANK YOU!