



# The chemistry between Newton and Schrodinger

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*“Those who educate children well are more to be honored than they who produce them; for these only gave them life, those the art of living well.”*

- Aristotle (384-322 BCE)

*“To me there has never been a higher source of earthly honor or distinction than that connected with advances in science.”*

– Sir Isaac Newton (1642-1727)

# Outline

- Why are we talking about this?
  - Understanding the world around us
  - Nobel Prize!
- The classical world through two slits
  - Particles: Newton, Lagrange and Hamilton
  - Waves: Huygens, Young
- It's 1926 and the world gets stranger: quantum mechanics
  - Bohr, Einstein, Schrodinger, Heisenberg, Born, Dirac, and Feynman
- Chemistry: a foot in two worlds

# The Nobel Prize in Chemistry 2013

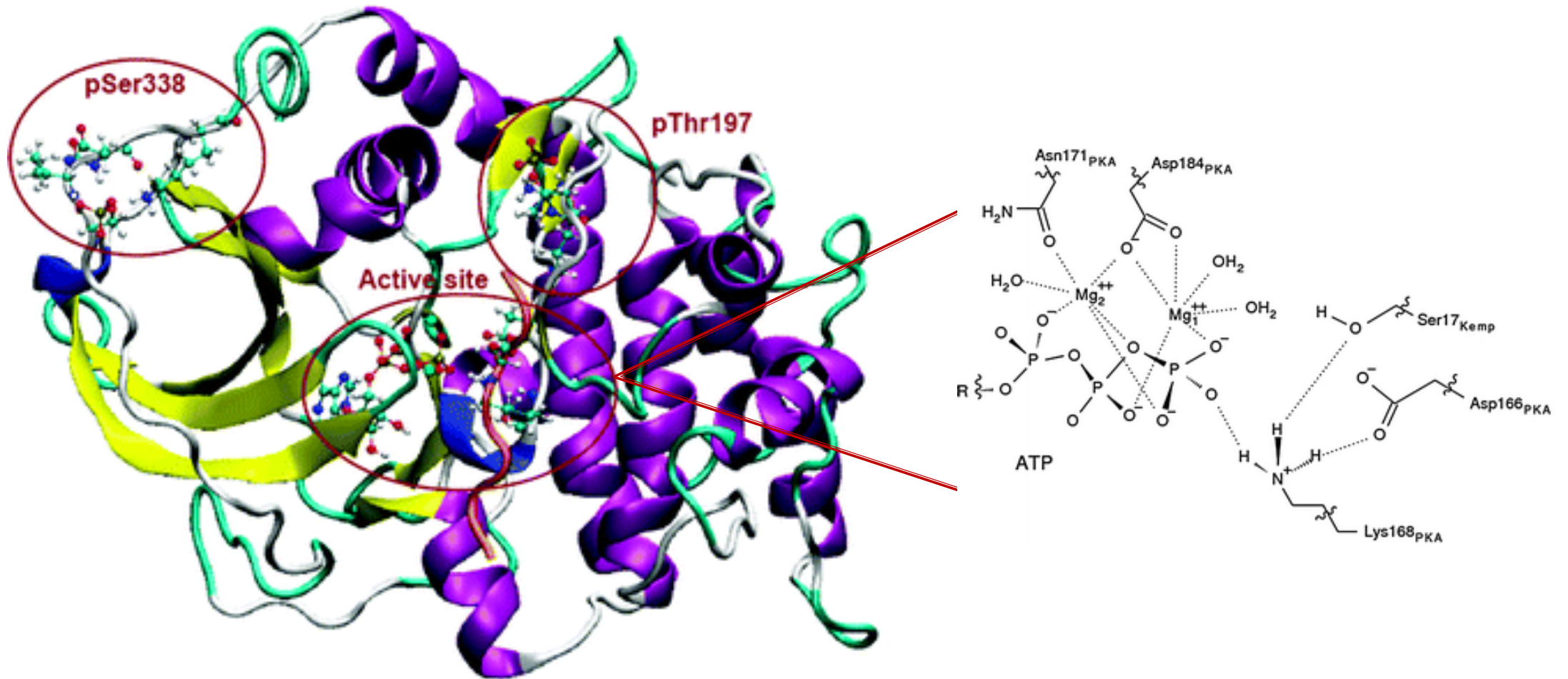
*“for the development of multiscale models for complex chemical systems”*



**Arieh Warshel (USC), Michael Levitt (Stanford Medicine), Martin Karplus (Harvard)**

*“...they managed to make Newton’s classical physics work side-by-side with the fundamentally different quantum physics.”*

# QM/MM study of protein kinase



Protein Kinase facilitates transfer of a phosphate ( $\text{PO}_4^-$ ) group:  
relevant to many auto-immune disorders

# Newton and Schrödinger's cat



# The methods of scientific research

- Unify: seek the underlying physics that unites disparate theories



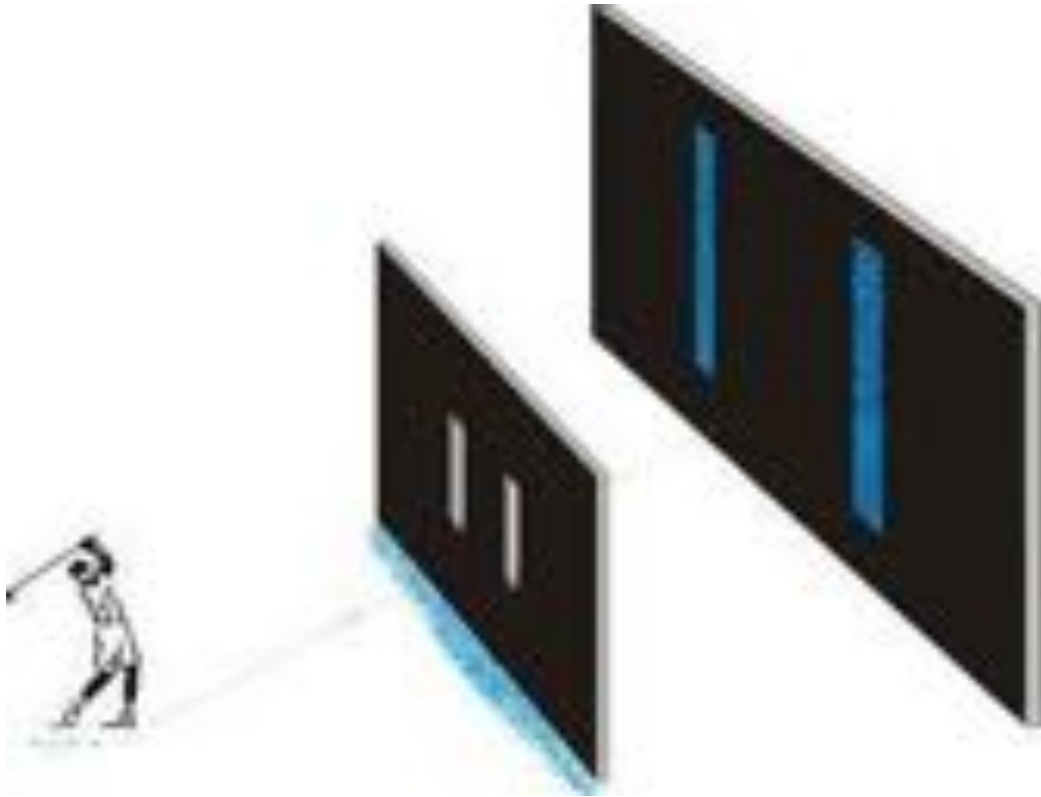
- Reformulate: understand an existing theory in a different way



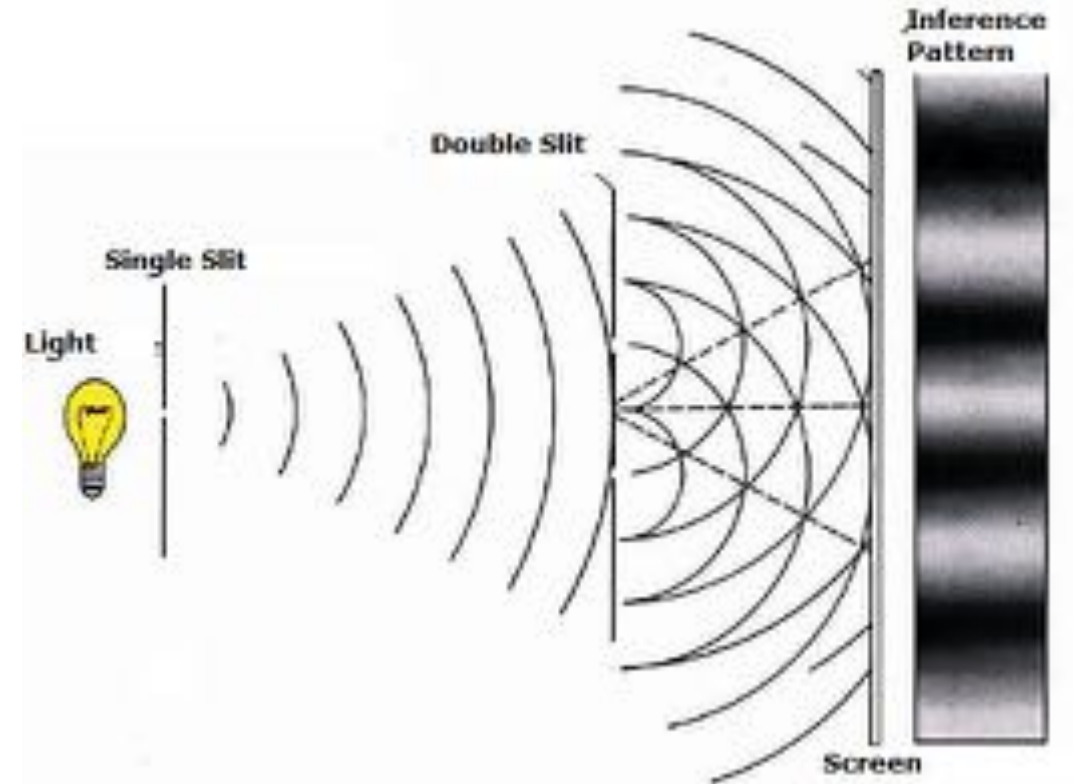
- Discover limits: identify new phenomena transcending current theories



# Classical double slit experiment



Classical Particles



Classical Waves

Thomas Young, 1803: set out to disprove Newton's corpuscular theory in favor of Huygen's wave theory of light.



# Things start to be 'quantum'

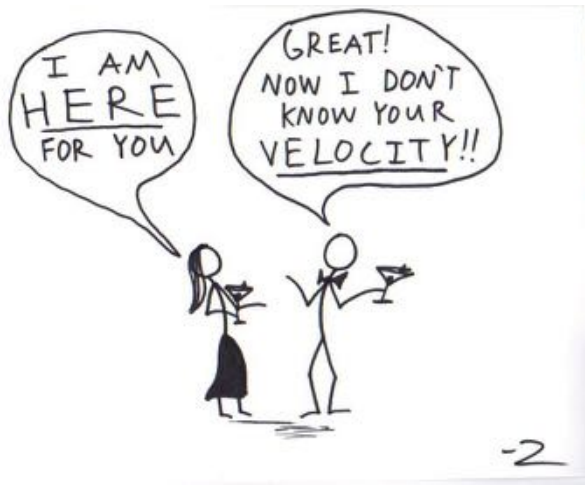
- Boltzmann (1877): energy levels of molecules may be discrete
- Heinrich Hertz and Einstein (1887): photoelectric effect
- Max Planck (1900): black-body radiation
- Neils Bohr (1913): on the constitution of atoms and molecules
- Louis Debroglie (1924): wave-particle duality
- 1926: Heisenberg develops matrix mechanics  
Schrödinger publishes wave equation



# Life after 1926

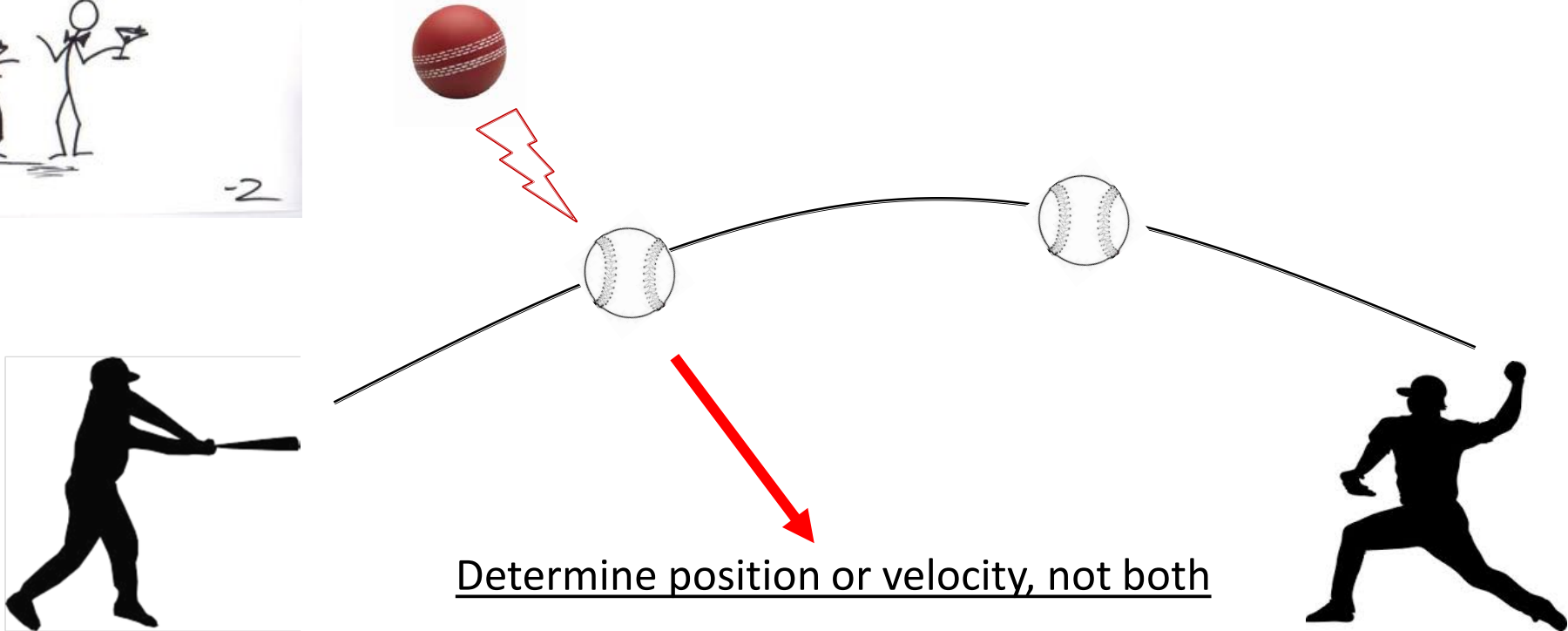
- 1927: Heisenberg uncertainty principle  
Dirac brings together QM and Einstein's special relativity  
Heitler and London pioneer quantum chemistry
- 1927-1940: Dirac, Pauli, Feynman – Quantum Field Theory
- 1975: Politzer, Gross and Wilczek – Quantum Chromodynamics
- 1979: Weinberg, Salam and Glashow – unified electroweak forces
- 2013: Confirmation of Standard model – theory of almost everything



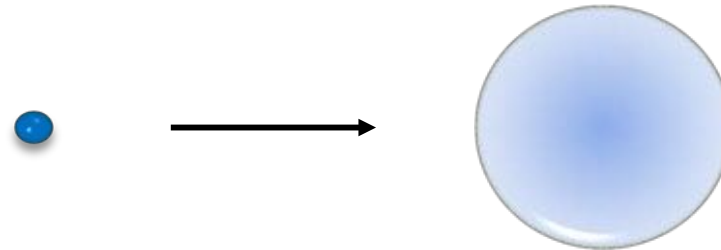


# Uncertainty principle

Consequence of Wave-Particle Duality!

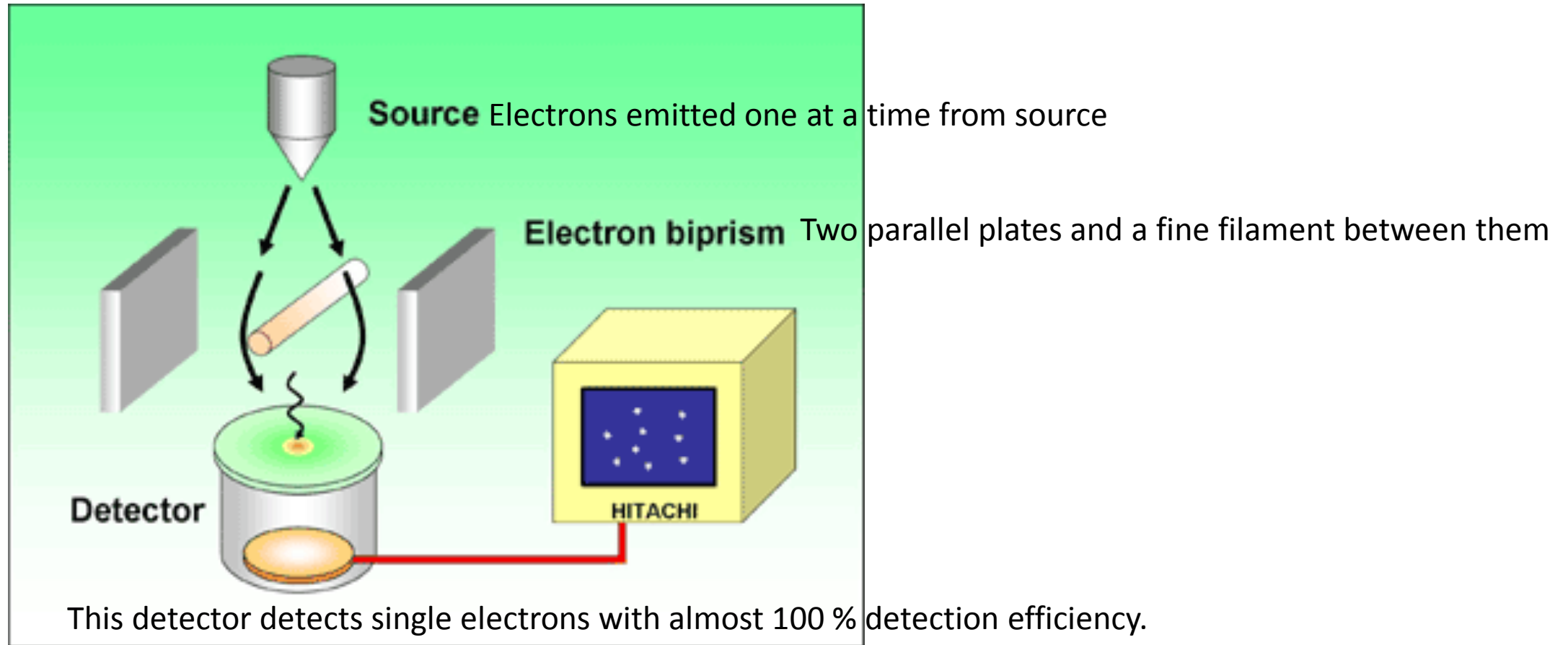


Determine position or velocity, not both



I, at any rate, am convinced that *He* does not throw dice - Einstein

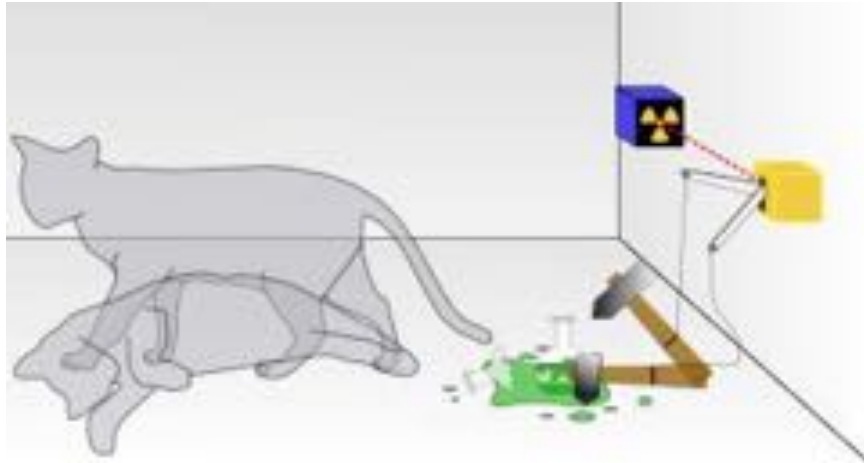
# Performing the quantum double-slit experiment



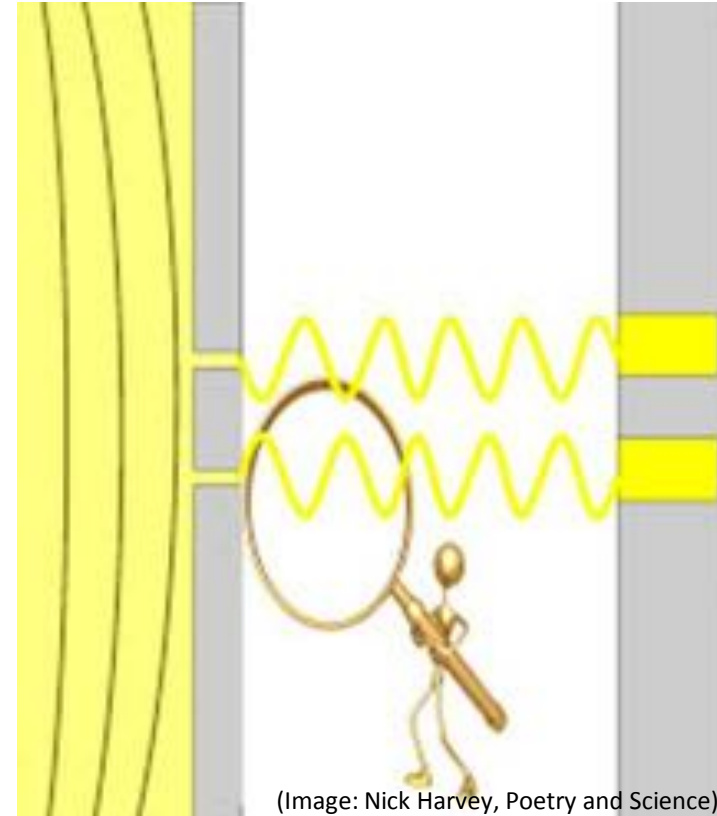
# Electron double-slit experiment

# The observer paradox

Copenhagen Interpretation of a measurement:



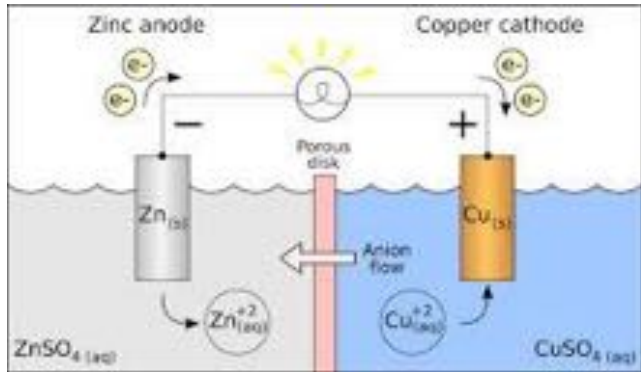
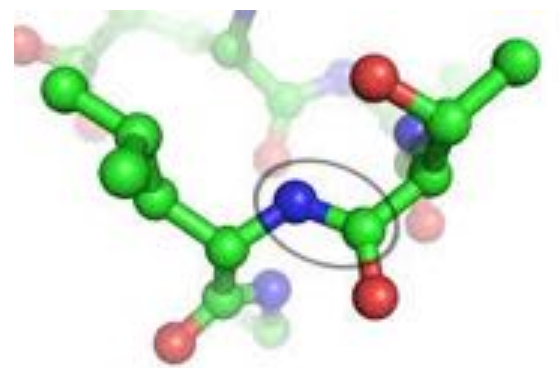
*Schrödinger's cat: reduction ad absurdum*



(Image: Nick Harvey, Poetry and Science)

The act of 'observation' interacts with the quantum system

# Connection to Chemistry?

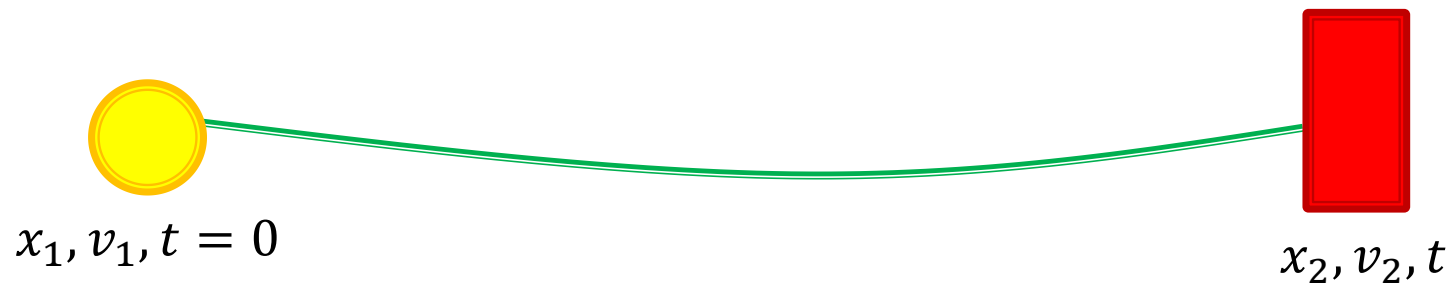


- Chemical reactions involve breaking, making, and changing bonds
- Changing bonds involves moving electrons and atoms: quantum mechanics.
- For bonds not explicitly involved in chemical reaction: classical mechanics.

What is a clever way to combine the two in one uniform framework?

# Classical mechanics

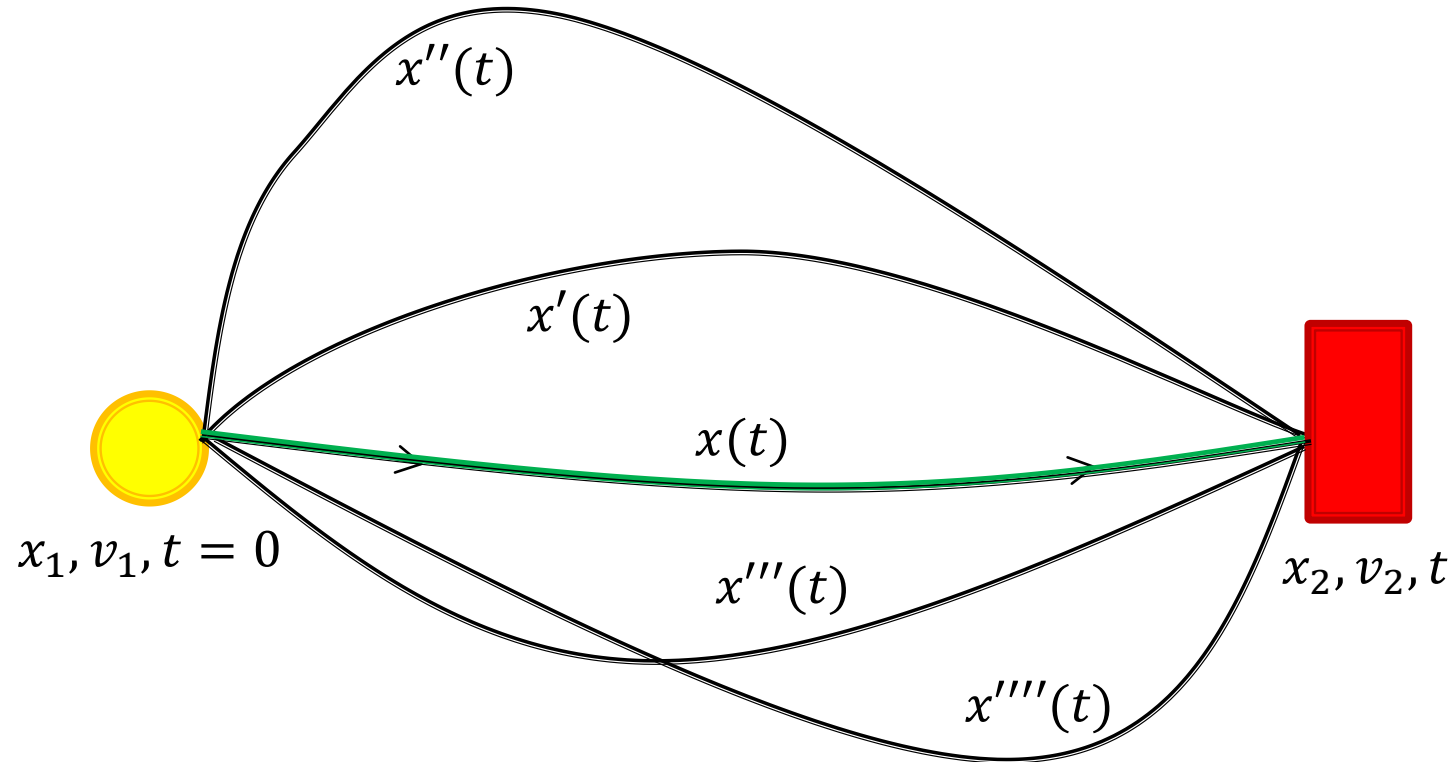
- Deterministic paths
  - Initial position
  - Initial velocity
  - Forces
- Newton's second law:  $F = ma$



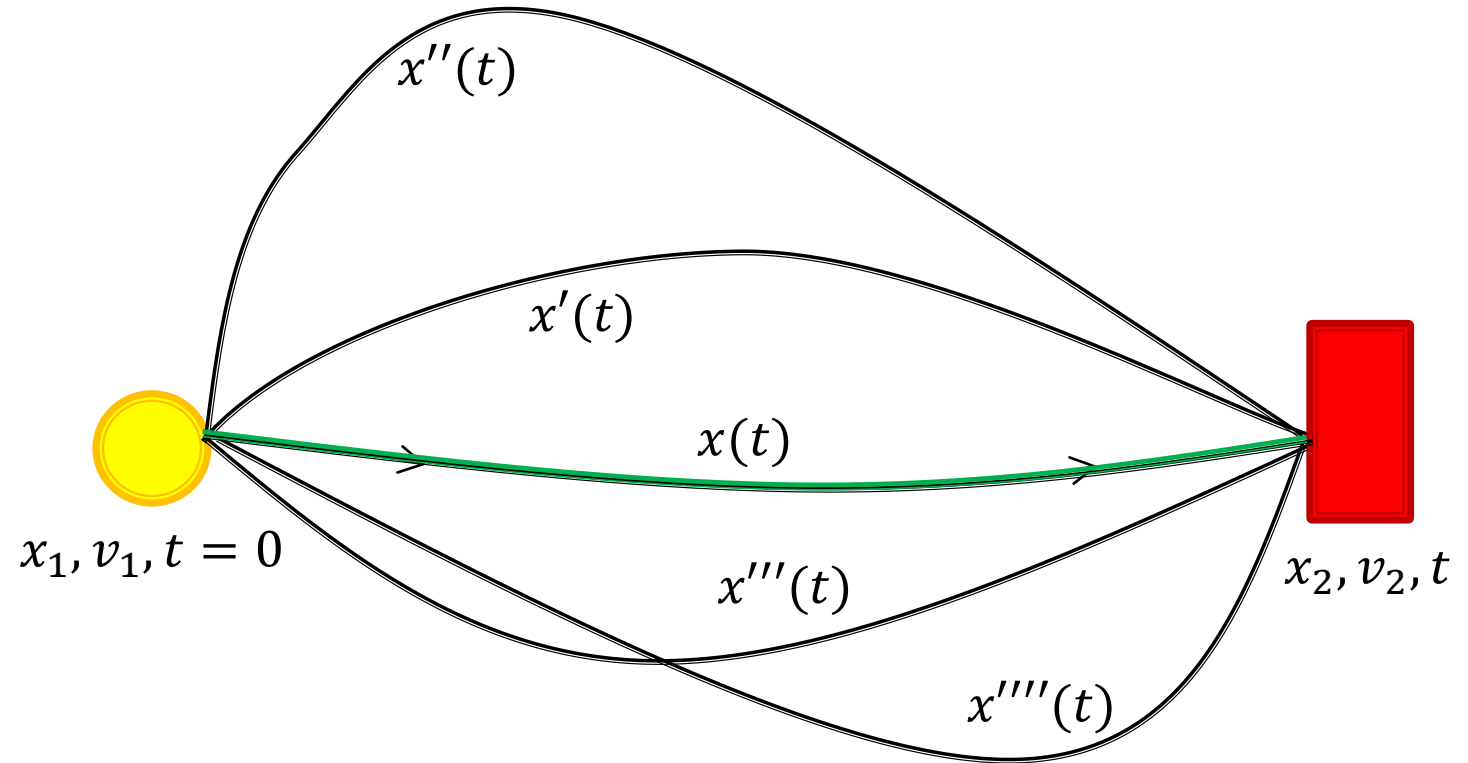


# Reformulate: Lagrange and Hamiltonian

- Lagrange introduce action: associate  $S[x(t)]$  with classical path  $x(t)$
- Hamilton's principal of least action:  $\delta S = 0$



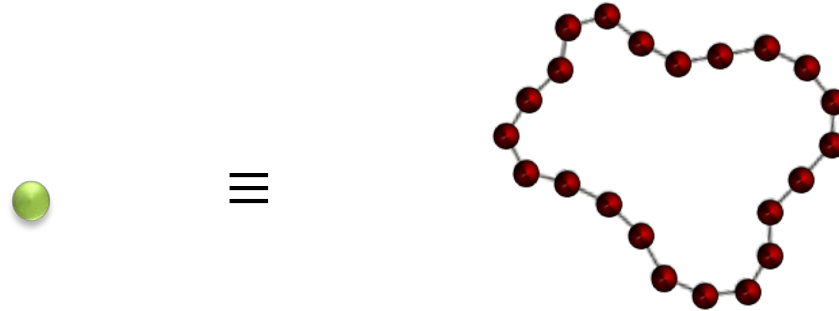
# Unify ideas: Feynman Path Integral



$$P((x_1, v_1, t = 0) \rightarrow (x_2, v_2, t)) \propto \sum_{\text{paths}} e^{\frac{iS[x_{\text{path}}(t)]}{\hbar}}$$

# Path-Integral representation of quantum mechanics

- A quantum particle behaves like a collection of classical particles



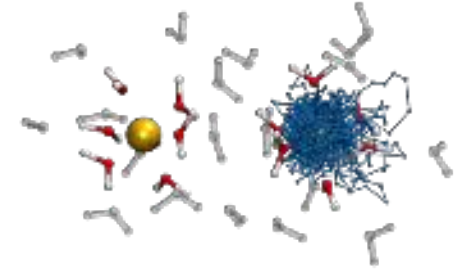
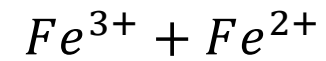
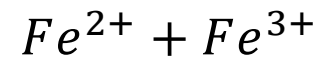
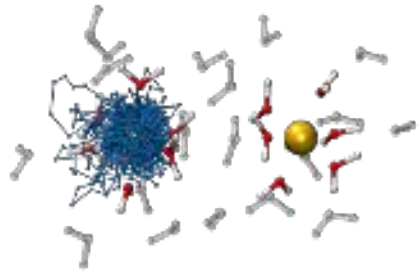
- A quantum particle that behaves like 1 classical particle is a classical particle
- The number of classical particles that describe a quantum particle depends on temperature and/or energy

# Dynamics of electron in water

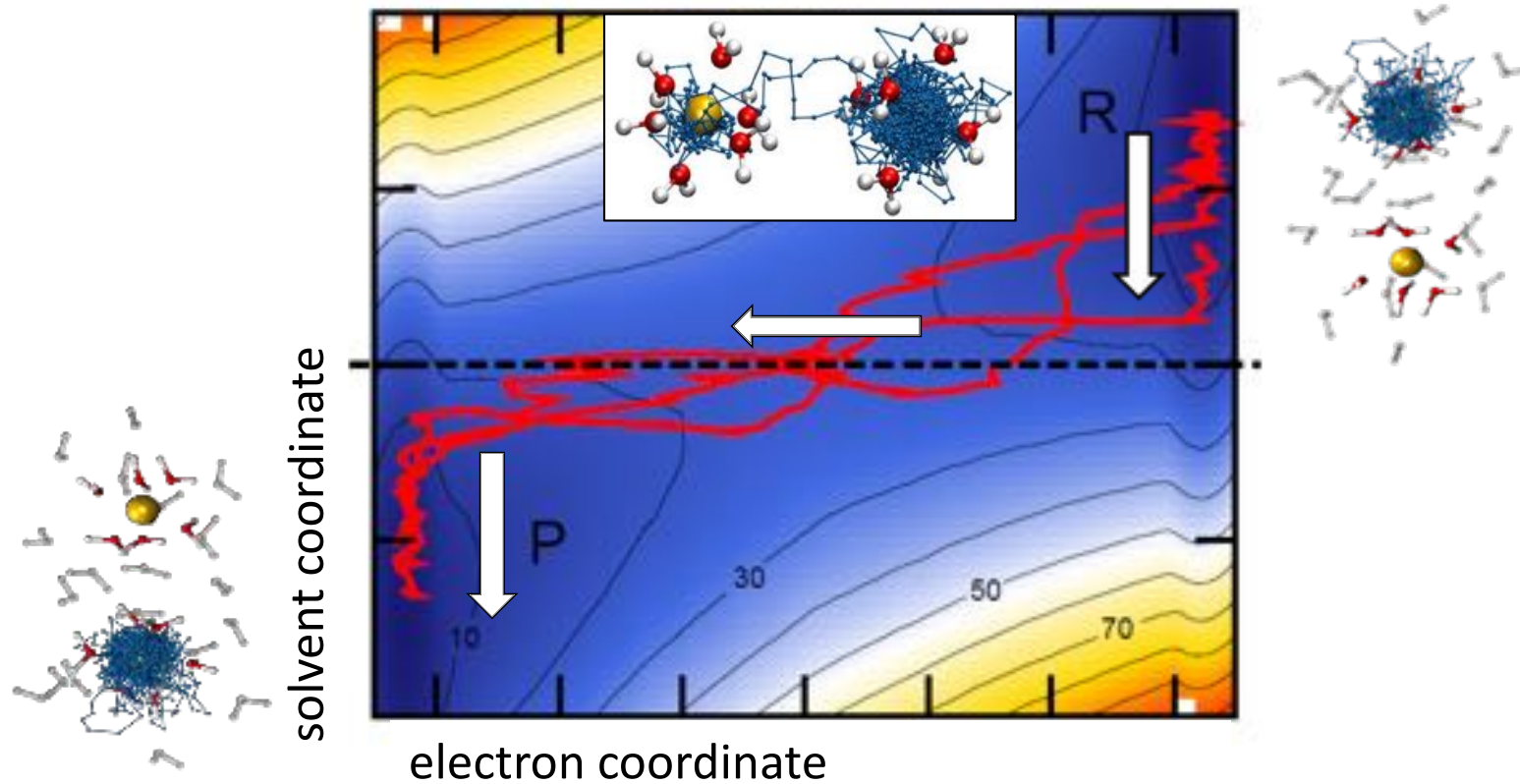
Solvated electron problem: important for all charged particle moving through solvent.

Applications: Battery and electrode design, charge transfer in condensed-phase reactions and many more.

# Electron transfer in solution



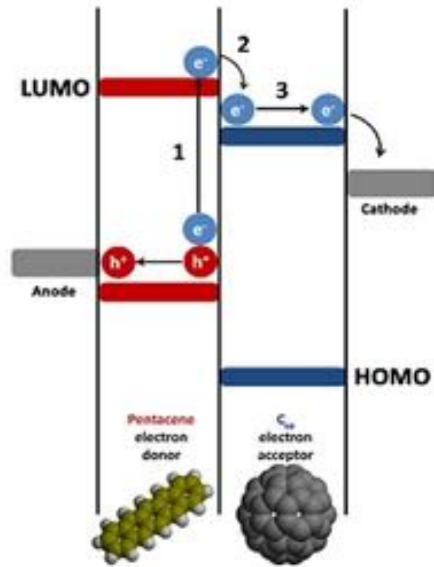
System size: 430 water molecules, 2 metal ions, 1024 path-integral 'beads' for electron.



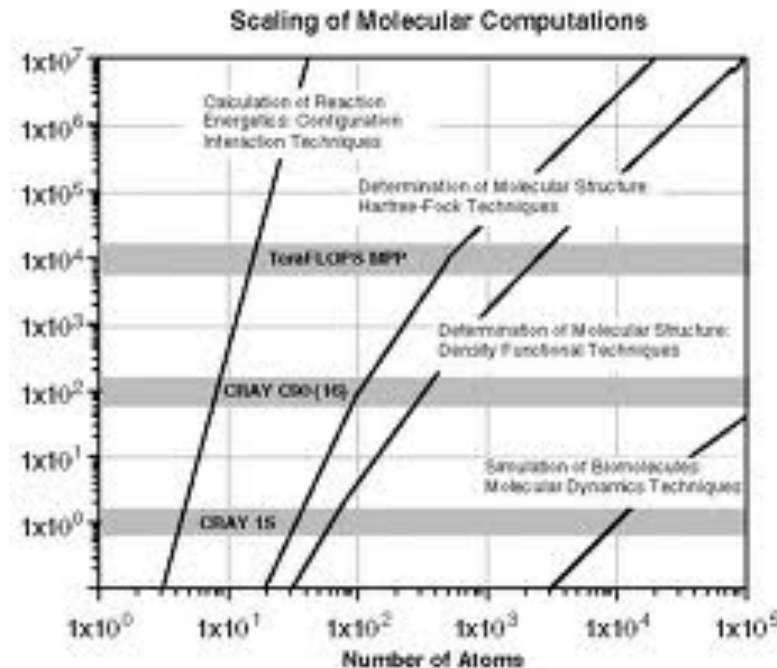
# Current research in theoretical chemistry



- Understanding structure-function relations in Biological systems



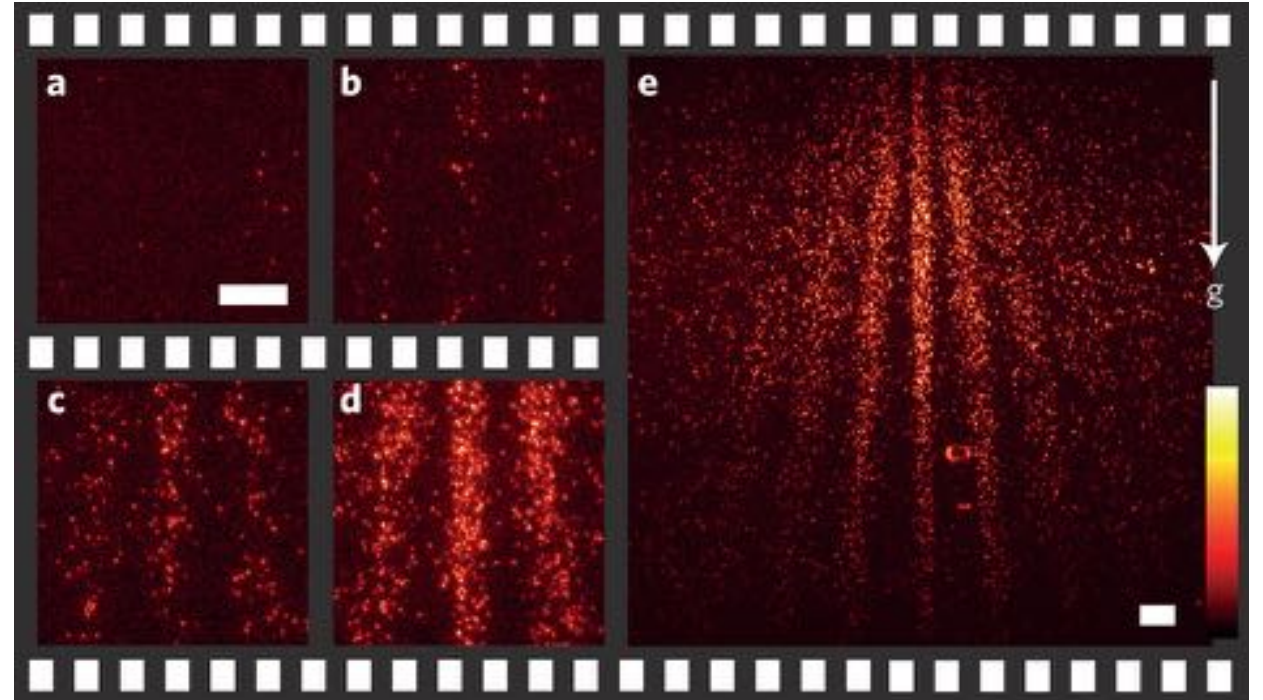
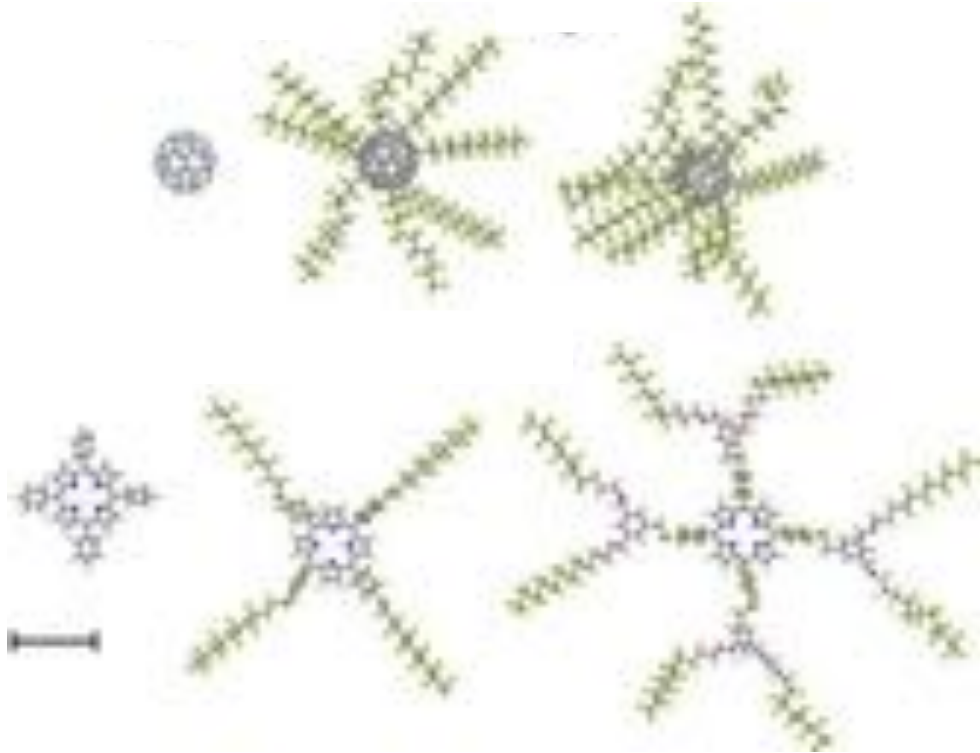
- Designing efficient renewable energy materials



- Computational complexity challenges

# Frontiers in quantum mechanics

How big is 'classical'?

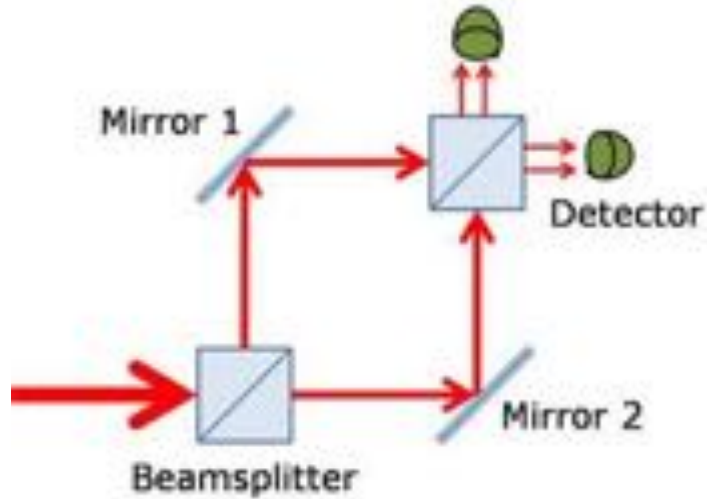


S. Gerlich et al, "Quantum interference of large organic molecules", *Nature* 2, 263 (2011).

T. Juffmann et al, "Real-time single molecule imaging of quantum interference", *Nature Nanotechnology*, 7, 297 (2012).

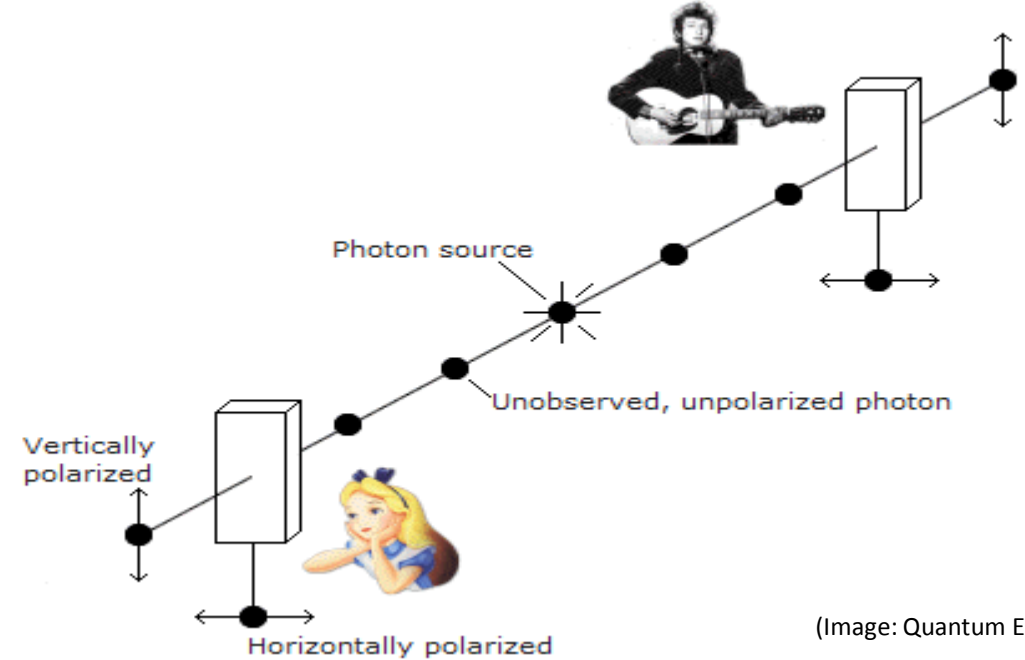
# Frontiers in quantum mechanics

## Role of observer: double-slit experiment



V. Jacques et al, "Experimental Realization of Wheeler's Delayed-Choice Gedanken Experiment", Science 315, 966 (2007).

## Einstein-Podolsky-Rosen (EPR)



(Image: Quantum Enigma)

## Quantum mechanical origin of gravity



Image: koya/shutterstock



‘Therefore, just as the doctor is said to heal a patient through the activity of nature, so a man is said to cause knowledge in another through the activity of the learner’s own natural reason and this is teaching’

- Thomas Aquinas (1225-1274)

THANK YOU!